## Introduction

In this paper, I discuss the implementation of a simple, single-hidden layer neural network for classification. Specifically, the model seeks to sort sixteen representations of English letters into nine distinct classes. My focus in this analysis will not be on the accuracy or efficiency of the model’s performance; rather, I will focus on the relationships between the hidden and output nodes after learning. By understanding how the hidden nodes subsequently affect the final predicted classifications, I gain a deeper understanding of the internal processes of neural networks.

As mentioned, the model consists of a single hidden layer. The input layer has eighty-one nodes, the single hidden layer has six, and the output layer has nine. As I am chiefly concerned with hidden node behavior, the number of hidden nodes was set at six, but not tested to see if it provided the best reduction in SSE.

My hypothesis for the hidden node interaction is that the hidden nodes will pick up not only clearly identifiable features of the inputs (e.g. long, straight, vertical lines), but also focus on patterns of *deactivated* inputs (e.g. letters with ample whitespace in the center region, such as D and O). Additionally, I believe that the output nodes will struggle to strongly predict across similar classes due to the relatively small number of hidden nodes-- class 1 (which contains the letters ‘B’ and ‘P’) and class 4 (containing “E” and “F”) will be too similar for the model to confidently distinguish between, for example.

## Data and Output Overview

### Data Overview

The input data consists of sixteen unique letters, A-P. Each letter is represented by a 9x9 grid, with the “filled-in” blocks working together to create an image of the letter. Of course, the 81-node input layer only “sees” the ‘K’ represented as a one-dimensional array (i.e. an 81x1 format). While the dimensionality of the layout may be different, with the 9x9 grid being easier for humans to interpret, it is possible to mentally map the structure of the input array back to the visual representation of the letter. In Figure 1, we see a table showing each letter, ordered by its desired class number, with the blue blocks signaling activation for each of the first 18 input nodes. Nodes X0 through X8 correspond to the top, 9-element row in our 9x9 matrix, while the next nine nodes correspond to the second row.



We can quickly see some patterns developing- letters that have a long, horizontal top row have nodes X0 through X8 activated with a one. We can also spot some potential challenges within classes- while ‘I’ and ‘J’ are both Class 5 representations, the letter I sees activations at nodes X2 through X6, while ‘J’ does not. These types of patterns continue throughout the 81 input nodes, but for length considerations, I will not include them all here.

### Output Overview

While I am not overly concerned with the accuracy or efficiency of the model results for the purposes of this paper, it is helpful to review the outputs to see where the model may have run into some difficulty in assigning the correct class. Table 1 below shows us the desired outputs from the model. The blue fields indicate the desired output of one for each input letter and output node/class.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Output Node | Class Name | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| o0 | A | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| o1 | B | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| o2 | C | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| o3 | D | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| o4 | E | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| o5 | I | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| o6 | K | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| o7 | L | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| o8 | M | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |

*Table 1*

In Table 2, we see the actual outputs. The model did exceptionally well on most input letters-- the correct class was identified for 15 of the 16 inputs. While the confidence is a bit lower for letters of the Class D (letters ‘O’ and ‘D’), it really only failed to make a correct choice for the sole member of Class C. We’ll investigate why identifying the letter ‘C’ might have caused some issues.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Output Node | Class Name | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| o0 | A | 0.91 | 0.01 | 0 | 0 | 0.04 | 0.04 | 0.01 | 0.91 | 0 | 0 | 0.03 | 0 | 0.05 | 0.08 | 0 | 0.02 |
| o1 | B | 0.02 | 0.95 | 0.01 | 0.03 | 0.03 | 0.05 | 0.92 | 0.03 | 0.03 | 0.02 | 0.06 | 0 | 0.01 | 0.01 | 0.03 | 0.89 |
| o2 | C | 0.03 | 0.05 | 0.03 | 0.03 | 0.02 | 0.03 | 0.05 | 0.03 | 0.07 | 0.07 | 0.03 | 0.03 | 0.04 | 0.04 | 0.03 | 0.04 |
| o3 | D | 0.01 | 0.08 | 0.02 | 0.86 | 0 | 0 | 0.08 | 0.01 | 0.07 | 0.06 | 0.01 | 0.08 | 0.12 | 0.12 | 0.86 | 0.06 |
| o4 | E | 0.05 | 0.04 | 0.04 | 0 | 0.93 | 0.92 | 0.04 | 0.05 | 0.03 | 0.03 | 0.02 | 0.07 | 0 | 0 | 0 | 0.04 |
| o5 | I | 0 | 0.04 | 0.06 | 0.02 | 0.02 | 0.03 | 0.04 | 0 | 0.92 | 0.92 | 0 | 0.05 | 0.01 | 0.01 | 0.02 | 0.02 |
| o6 | K | 0.03 | 0.03 | 0.01 | 0.01 | 0.01 | 0.01 | 0.03 | 0.03 | 0 | 0 | 0.89 | 0.07 | 0.04 | 0.01 | 0.01 | 0.04 |
| o7 | L | 0.01 | 0 | 0.02 | 0.01 | 0.02 | 0.01 | 0 | 0.01 | 0.05 | 0.05 | 0.08 | 0.9 | 0.02 | 0.01 | 0.01 | 0 |
| o8 | M | 0.06 | 0 | 0.01 | 0.07 | 0 | 0 | 0 | 0.07 | 0.01 | 0.01 | 0.06 | 0.01 | 0.92 | 0.9 | 0.07 | 0 |

*Table 2*

## Hidden Node Interpretation

In Table 3, I present the final Hidden-to-Output weights in “indexed” form-- rather than examining the actual weights, I divided each cell by the average of its row (the rows represent the hidden nodes) and multiplied the result by -100 (to account for average weights being negative-- this way, positive numbers mean positive weights and negative numbers represent negative weights, to avoid any confusion in interpretation). The purpose in converting to an index was to focus on the relationships between the nodes, rather than getting caught up in the specific weight values.

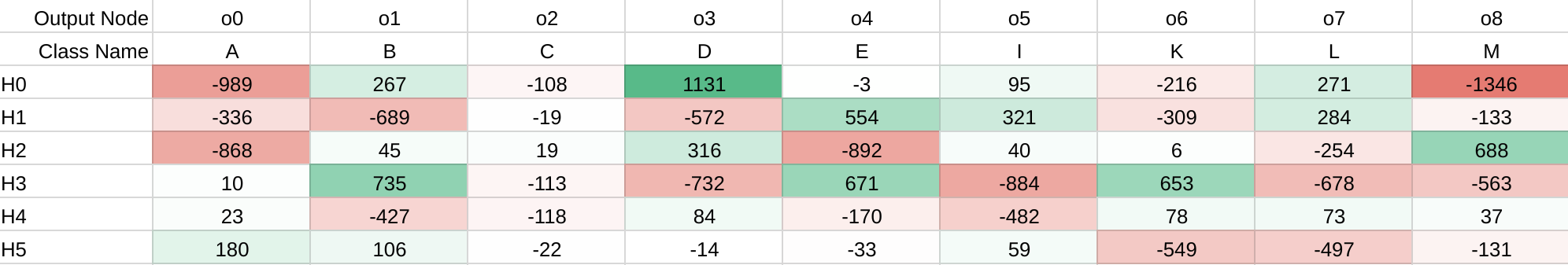


Table 3

In trying to determine which features are being represented by each hidden node, we can reference the above table and see the relationships the weights are having on the various output nodes. For instance, node H0 is providing strong activation weights to the output node representing class D, along with lesser, but still strong, activations to the nodes for classes B and L. Conversely, node H0 is providing strong, negative weights to output classes A and M. At first blush, it appears that node H0 is picking up on input letters that have horizontal bars in the middle of the image, but also are activated along the bottom row.

This type of reasoning can be misleading, however-- it is important to remember that this type of network learns *global* patterns, not *local* ones. In essence, the network is not learning that class A, for example, has a horizontal line, it is learning the overall patterns of the input images. While the horizontal line is a part of that pattern, the network needs the overall pattern to understand what it is “seeing”.

This distinction between global and local patterns may help us understand why the class C, containing only the same letter, caused trouble for the network. The global pattern of C is similar to several other letters (D, G, and O, for starters). The network was “smart” enough to know that it did not fit cleanly into any of those classes, but it could not reliably recognize it as its own class. The network did not commit on way or the other-- the weights to output node o3 are all relatively low, and the letter C did not activate any of the output nodes.

Other hidden nodes follow the same pattern, activating a small number of nodes in a significant, positive way, while providing strong, negative weights to other. Not all nodes follow this pattern, however-- node H4 seems to serve mainly as a “spoiler” node. It does not provide high activations to any output nodes, but passes negative weights (from low activations) to classes B and I.

## Conclusions

Revisiting my hypothesis for the hidden node interaction, I thought that the hidden nodes would pick up not only clearly identifiable features of the inputs (e.g. long, straight, vertical lines), but also focus on patterns of *deactivated* inputs (e.g. letters with ample whitespace in the center region, such as D and O). Additionally, I believed that the output nodes would struggle to strongly predict across similar classes due to the relatively small number of hidden nodes.

Broadly, this turned out to be true, though I was incorrect with regards to some of the specifics. The network had no issues distinguishing between class 1 and class 4, but did have issues with class 2. While the network did pick up on input patterns, it did so in a global way, not a local one. We could not, as an example, pass the letter P in a way that it only activated inputs found in the lower-right quadrant of a 9x9 representation and expect the network to understand that those local patterns create the same letter as the full-grid version.